Energetic particle transport in the magnetosphere and atmosphere

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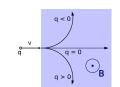
HESPERIA - Summer School Kiel, 29 August - 2 September 2016

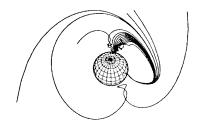
Motivation

- Understand the high-energy processes at the Sun that accelerate particles to cosmic ray energies
- For this task cosmic ray measurements in space and on Earth are used
- For the interpretation of ground based detectors the transport in the magnetosphere and in the atmosphere must be known

Transport in the Geomagnetosphere

- Moving charged particles are deviated in magnetic fields (Lorentz Force)
- Positive particles deflect one way and negative particles the other way
- Charged particles entering the Earth magnetic field describes complex trajectories
- Charged particles must have a minimal energy to reach the top of the Earth's atmosphere





Transport in the Atmosphere

- Interactions of primary cosmic rays with electrons and nuclei of atoms and molecules in atmosphere
- As a result composition of radiation changes (secondary cosmic rays)
- All particles suffer energy losses through hadronic and/or electromagnetic processes.



Nomenclature and defintions I

Energy unit:

$$1 \text{ eV} = 1.6 \cdot 10^{-19} \text{ J}$$

1 electron Volt (eV) is the kinetic energy a particle with charge *e* gains by being accelerated through a potential difference of 1 Volt.

 $keV (10^3 eV), MeV (10^6 eV), GeV (10^9 eV)$

Total energy of a particle, E_T :

$$E_T = E_{kin} + m_0 c^2 = mc^2 = \gamma m_0 c^2$$

 E_{kin} : kinetic energy

m₀: rest mass

c: speed of light

$$\gamma$$
: Lorentz factor, $\gamma = \frac{1}{\sqrt{1-(\frac{\nu}{c})^2}}$

Rest mass of nucleons:

$$m_p=938.272\,\mathrm{MeV}/\mathit{c}^2$$

$$m_n = 939.565 \,\mathrm{MeV}/c^2$$

Nomenclature and defintions II

 E_T is related to the particle momentum, p, by

$$E_T = \sqrt{p^2 c^2 + m_0^2 c^4}$$

Magnetic rigidity, R

$$R = \frac{p \cdot c}{Z \cdot e}$$

where $Z \cdot e$ is the charge of the particle.

Unit of R is Volt. Convinient units are MV (106V), GV (109V)

The rigidity of a particle is a measure of its resistance to a magnetic force.

Paritcles with the same rigidity, charge sign and initial conditions have identical trajectories in a static magnetic field.



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Nomenclature and defintions III

Conversion from kinetic energy per nucleon, E_A , to rigidity, R

$$R = \frac{A}{Z}\sqrt{(\gamma^2 - 1)} \cdot E_{0A}$$

where A is the atomic number, Z is the atomic charge, γ is the Lorentz factor, and E_{0A} is the rest mass energy per nucleon.

Computation of the Lorentz factor, γ

from either the cosmic ray kinetic energy per nucleon, E_A :

$$\gamma = \frac{E_A + E_{0A}}{E_{0A}}$$

or from the cosmic ray rigidity, R:

$$\gamma = \sqrt{(\frac{R \cdot Z}{A/E_{0A}})^2 + 1}$$

Conversion rigidity ←→ kinetic energy for protons

Conversion kinetic energy to rigidity for proton:

Conversion rigidity to kinetic energy, E_{kin} , of a proton:

$$R = \sqrt{(E_{kin} + E_0)^2 - E_0^2}$$

$$E_{kin} = \sqrt{R^2 + E_0^2 - E_0}$$

where

R: rigidity in [MV]

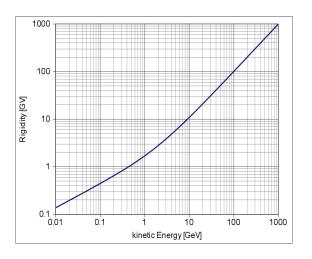
 E_{kin} : kinetic energy of proton

in [MeV]

 E_0 : rest mass of proton,

 $E_0 = 938.27 \text{ MeV}$

Rigidity vs. kinetic energy for protons



1 GV [≙] ~450 MeV

Transport in the Magnetosphere

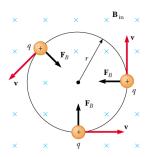
Motion of charged particles in static and uniform magnetic field I

Lorentz force:

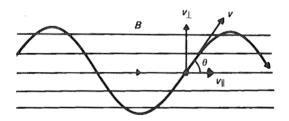
$$\vec{F} = q \cdot \vec{E} + q \cdot \vec{v} \times \vec{B}$$

Cyclotron radius:

$$\vec{r}_{cy} = \frac{m}{Z \cdot e} \frac{\vec{B} \times \vec{v}}{B^2}$$



Motion of charged particles in static and uniform magnetic field II



 \vec{B} : uniform magnetic field

 \vec{v} : speed of particle

 $v_{||}$: speed rectangular to \vec{B}

 v_{\perp} : speed parallel to \vec{B}

 θ : pitch angle, i.e. angle between \vec{v} and \vec{B}



Magnetic fields

Units:

- 1 Gauss [G] = 100 000 Nanotesla [nT] = 105 nT
- 1 Gamma [γ] = 1 Nanotesla [nT] 1 T = 1 $\frac{V_S}{m^2}$

Interplanetary magnetic field near Earth: typical $B_{IMF} \approx 5 \text{ nT}$

$$B_{equator} \sim 0.3~Gauss = 30'000~\text{nT}$$

$$B_{pole}\sim 0.6~Gauss=60'000~\mathrm{nT}$$

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Magnetic fields

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$$1~T=1\tfrac{Vs}{m^2}$$

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typical
$$B_{IMF} \approx 5 \, \text{nT}$$

$$B_{equator} \sim 0.3~Gauss = 30'000~nT$$

$$B_{pole} \sim 0.6 \, Gauss = 60'000 \, \mathrm{nT}$$

Cyclotron radius

Interplanetary magnetic field near Earth:

$$r_{cy}[AU] = rac{R[V]}{4.5 \cdot 10^{10} \cdot B[nT]}$$

B = 5 nT, R = 1.0 GV $ightarrow r_{cy}$ = 0.005 AU

$$r_{cy}[cm] = \frac{R[V]}{300 \cdot B[gauss]}$$

$$B = 0.3$$
 gauss, $R = 1.0 \text{ GV} \rightarrow r_{cv} = 110 \text{ km} \triangleq 0.02 \text{ Re}$

Charged particle equation of motion in a magnetic field

$$\gamma m_0 \dot{\vec{v}} = q \cdot (\vec{v} \times \vec{B})$$

where

 $\dot{\vec{v}}$ particle acceleration

q charge of particle

m₀ particle's mass at rest

 \vec{v} particle velocity

 \vec{B} magnetic field vector

Determination of cosmic ray particle trajectories Numeric integration of the equation of motion



Charged particle equation of motion in a magnetic field

$$\gamma m_0 \dot{\vec{v}} = q \cdot (\vec{v} \times \vec{B})$$

where

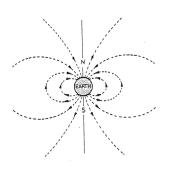
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- \vec{v} particle velocity
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Determination of cosmic ray particle trajectories: Numeric integration of the equation of motion



Earth magnetic field I

First approach: Description of the Earth magnetic field by a geocentric magnetic dipole

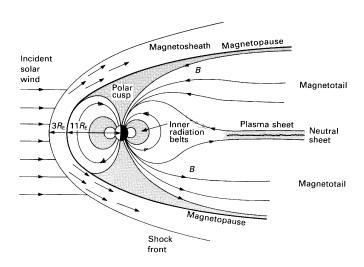


$$|\vec{B}| = \frac{M}{r^3} \cdot \sqrt{1 + 3\sin\lambda^2} \propto \frac{1}{r^3}$$

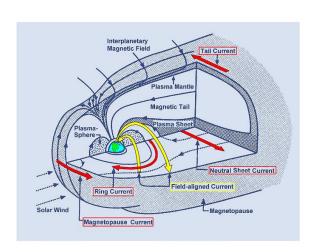
where

- M geomagnetic moment $(M = 8.1 \cdot 10^{25} \,\text{Gauss cm}^3),$
- r radial distance from Earth's center,
- λ geomagnetic latitude

Earth magnetic field II



Earth magnetic field III: Magnetospheric currents



$$B \propto \frac{l}{r}$$

Earth magnetic field IV: Magnetic field models

Main field generated by sources in the Earth's interior:

International Geomagnetic Reference Field (IGRF)

International Union of Geodesy and Geophysics (IUGG) / International Association of Geomagnetism and Aeoronomy (IAGA)

Magnetic field generated by current systems:

Tsyganenko89, Tsyganenko96, Tsyganenko2001



Earth magnetic field V: IGRF

- The IGRF model is a Gauss spherical harmonic model that describes Earth's main magnetic field and its secular variation
- Gauss coefficients are derived from magnetic field measurements (geomagnetic stations, magnetometers on ships, and satellite measurements)
- Every 5 years a new set of Gauss coefficients g_n^m and h_n^m are published by International Association of Geomagnetism and Aeronomy (IAGA)
- The 12th Generation IGRF will accept dates in the range 1900 to 2025



Earth magnetic field VI: External magnetospheric field model

The Tsyganenko89 model provides 7 states of the magnetosphere corresponding to different levels of geomagnetic activity

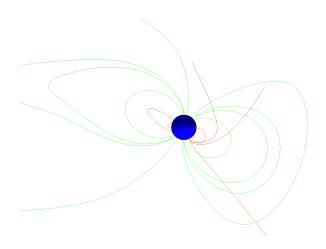
The different states, *lopt*, are described by the K_p -index as follow:

lopt	1	2	3	4	5	6	7
Kp	0,0+	1-,1,1+	2-,2,2+	3-,3,3+	4-,4,4+	5-,5,5+	>6-

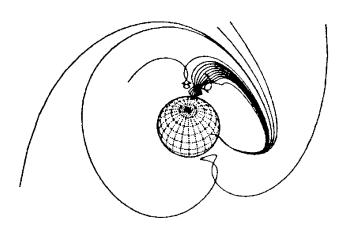
Trajectory computation: Solution method

- Determination of trajectories by numeric integration of the equation of motion by using a geomagnetic field model.
- Path of a negative charged particle with rigidity, R, is identical to path of a positive charged particle but with reverse sign of the velocity vector.
- Trajectory is computed in the reverse direction, i.e. starting point = above the observation location (20 km asl).
- · Vertical incidence at the top of the atmosphere.

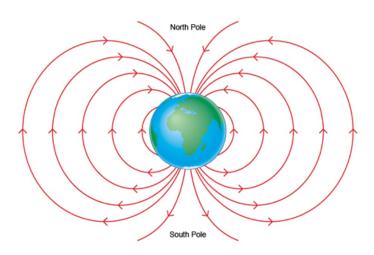
CR particle in Earth's magnetic field



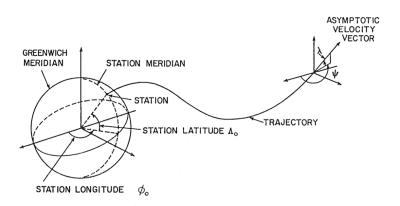
Allowed / forbidden trajectories



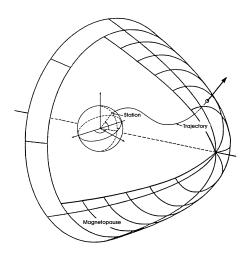
Minimal rigidity for access



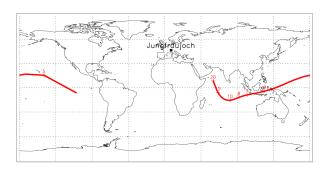
Definition asymptotic direction



Definition asymptotic direction



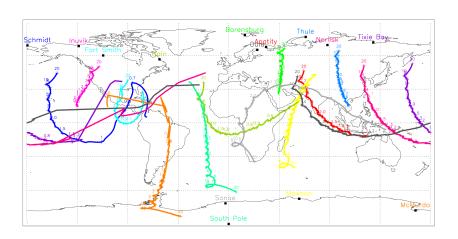
Asymptotic directions for the location Jungfraujoch



Jungfraujoch:

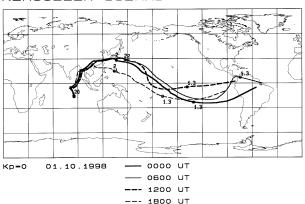
Geographic latitude: 46.55° N Geographic longitude: 7.98° E Altitude: 3570m asl

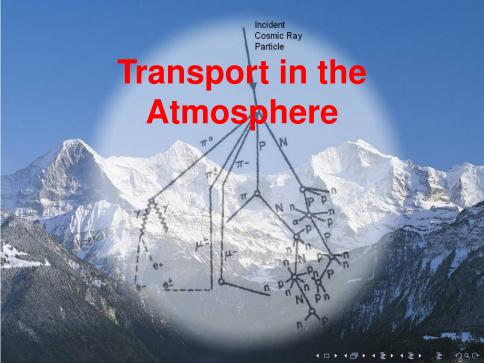
Computed asymptotic directions for polar neutron monitor locations

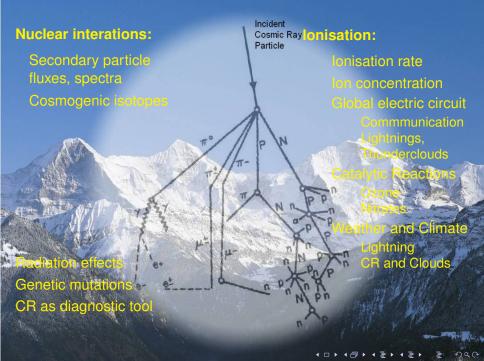


Asymptotic directions vs. time

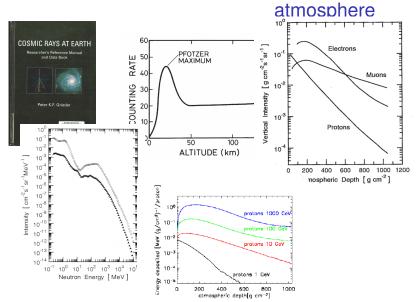
KERGUELEN ISLAND



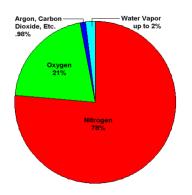




Cosmic Rays in the Earth's

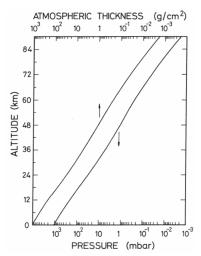


Earth's atmosphere I: Chemical composition



Chemical element	Proportion by Volume
Nitrogen	\sim 78 %
Oxygen	\sim 21 %
Argon	\sim 1 %

Earth's atmosphere II: Atmospheric thickness / atmospheric depth



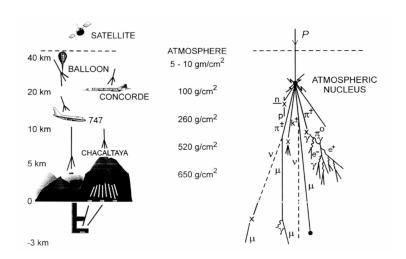
Atmospheric depth:

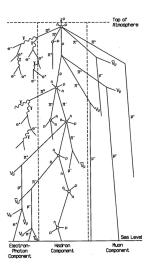
20'000 m asl: $\sim 50 \text{ g} \cdot \text{cm}^{-2}$ 11'000 m asl: $\sim 250 \text{ g} \cdot \text{cm}^{-2}$ Sea level: $\sim 1'033 \text{ g} \cdot \text{cm}^{-2}$

 $1'033 \text{ g} \cdot \text{cm}^{-2} = 1'013 \text{ mbar} = 760 \text{ mmHg}$

Earth's atmosphere III: Models of Earth's atmosphere

- U.S. Standard Atmosphere
- International Standard Atmosphere (ISA)
- NRLMSISE 2000 model





The "standard picture"

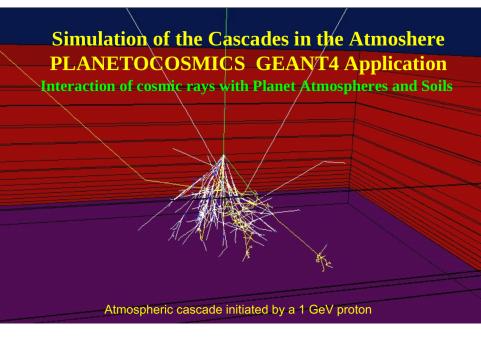
Present solution to the problem: cascade programs

e.g. PLANETOCOSMICS (GEANT4 application)

Technique:

- 1 calculate $\bar{N}_{kj}^{k_0}(h,R_0,\vartheta)$ i.e. the number of secondaries of type k, in energy interval $E_i + \Delta E_i$, in zenith angle interval $\vartheta_j + \Delta \vartheta_j$, produced on average at atmospheric depth h by a primary particle of type k_0 , penetrating the Earth's atmosphere with rigidity R_0 under a zenith angle ϑ_0
- 2 take into account cutoff information
- 3 integrate over respective primary particle spectrum

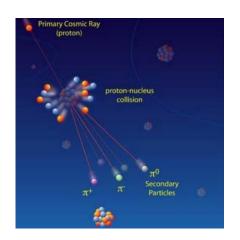


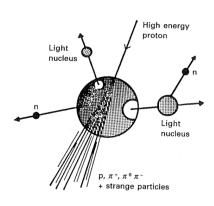


Basic physics background

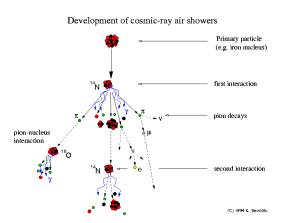
"interaction of particles and radiation with matter"

Nuclear Interactions I



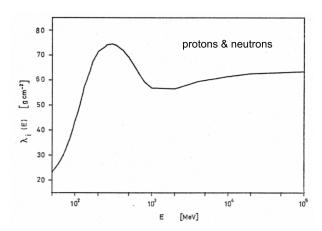


Nuclear Interactions II



Nuclear Interactions III

The hadronic interaction mean free path λ_i (g cm⁻²)



Nuclear Interactions IV: Energy Transport

A hadron having an initial energy E_0 , undergoing n interactions with a mean inelasticity, < k >, will retain on average an energy, E, of

$$E = E_0 \cdot (1 - \langle k \rangle)^n$$

typically
$$< k > \approx 0.5$$

Production of Pions & Muons I

Of all the secondaries, pions (π^+, π^-, π^0) are the most abundant

Mass:
$$m_{\pi^0} = 134.97 \text{ MeV/c}^2$$

$$m_{\pi^{\pm}} = 139.57 \text{ MeV/c}^2$$

Very short mean life times:
$$\pi^0$$
: $\tau \approx 10^{-16}$ s $\pi^0 \Rightarrow \gamma + \gamma$ π^{\pm} : $\tau \approx 2.6 \cdot 10^{-8}$ s

$$au^+$$
 $au \approx$ 2.6 · 10 ° S
$$au^+ \Rightarrow \mu^+ + \nu_\mu \\ au^- \Rightarrow \mu^- + \bar{\nu}_\mu$$

Decay within meters!

Interaction mean free path in air: \sim 120 g cm⁻²



Production of Pions & Muons II

Mass: $m_{\mu} = 105.658 \text{ MeV/c}^2$

Mean lifetime: $\tau \approx 2.197 \cdot 10^{-6} \text{ s}$

$$\mu^+ \Rightarrow \mathbf{e}_+ + \nu_{\mathbf{e}} + \bar{\nu}_{\mu}$$
 $\mu^- \Rightarrow \mathbf{e}_- + \bar{\nu}_{\mathbf{e}} + \nu_{\mu}$

Although their lifetime without relativistic effects would allow a half-survival distance of only about 500 m at most, the time dilation effect of special relativity allows cosmic ray secondary muons to survive the flight to the Earth's surface.

Muons

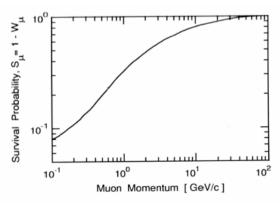


Figure 1.6: Survival probability of muons originating from an atmospheric depth of 100 $\rm g/cm^2$ to reach sea level, versus muon momentum.

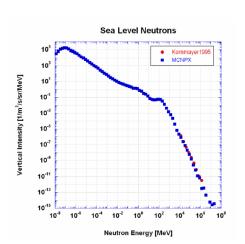
Differential Proton Spectra

Tabelle 9 Differentielles Protonenspektrum in der atmosphärischen Tiefe $h=1033~{\rm g~cm^{-2}}$ für mittlere Sonnenaktivität und $R_{\rm CV}\approx 4.4~{\rm GV}$

	$\Phi_p(E, \theta, h = 1033 \text{ g cm}^{-2})$ [Protonen/cm ² sterad sec MeV] Zenitwinkel				
Vinationha Enousia					
Kinetische Energie [MeV]	0°-15°	15°-30°	30°-45°	45°-60°	60°-90°
50- 100	0.51 <i>E</i> 06	0.39E-06	0.16E-06	0.44E-06	0.66 <i>E</i> —-07
100~ 200	0.19E - 06	0.33E-06	0.19E - 06	0.18E - 06	0.31E-06
200- 400	0.43E-06	0.13E - 06	0.83E - 07	0.54E-07	0.58E - 08
400- 600	0.21E-06	0.59E - 07	0.31E - 07	0.0	0.76E-08
600- 800	0.12E-06	0.41E-07	0.36E-07	0.19 <i>E</i> —07	0.0
800- 1000	0.90E-07	0.32E - 07	0.22E - 07	0.53E - 08	0.0
1000 1250	0.66E - 07	0.59E-07	0.69E - 08	0.0	0.0
1250- 1500	0.47E-07	0.17E-07	0.14E-07	0.0	0.0
1500- 1750	0.45E-07	0.41E-07	0.11E-07	0.0	0.0
1750- 2000	0.60E-07	0.26E-07	0.51E-08	0.33E-08	0.0
2000~ 3000	0.29E07	0.13E-07	0.23E - 08	0.17E - 08	0.0
3000- 5000	0.10E-07	0.19E - 08	0.81 E09	0.0	0.0
5000- 7500	0.21E - 08	0.0	0.0	0.0	0.0
7500 10000	0.23E - 09	0.11E - 08	0.0	0.0	0.0
10000 15000	0.15E-09	0.0	0.0	0.0	0.0
15000- 20000	0.16E-09	0.0	0.0	0.0	0.0
20000- 30000	0.0	0.0	0.0	0.0	0.0
30000 40000	0.29E-10	0.0	0.0	0.0	0.0
40000- 50000	0.0	0.0	0.0	0.0	0.0
50000- 75000	0.0	0.0	0.0	0.0	0.0
75000-100000	0.0	0.0	0.0	0.0	0.0

Differential Neutron Spectra

(still considerable uncertainties!)



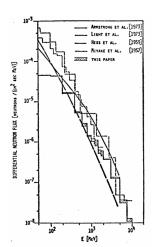
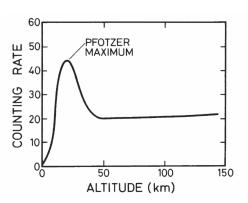


Figure 1. Differential neutron flux at atmospheric depth h = 650 q cm⁻².

Hagmann et al., 2007

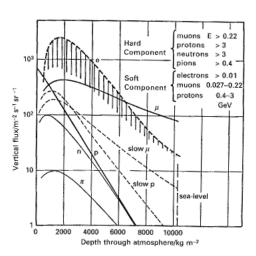
Vertical Development I



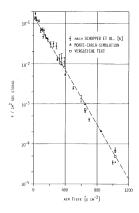
The production of secondary components becomes significant at \sim 55 km and reaching a maximum (Pfotzer maximum) at \sim 20 km.

Vertical Development II

Different species of secondary cosmic rays in the atmosphere



Attenuation of Protons in the Atmosphere



Attenuation of vertical intensity > 1 GeV proton

Altitude dependence of hadron flux, I:

$$I(0^{\circ}, X_2) = I(0^{\circ}, X_1) \exp{(-rac{X_2 - X_1}{\lambda})}$$

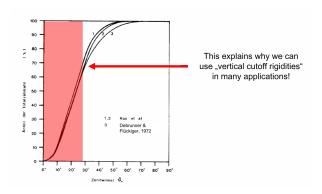
where $X_2 \ge X_1$, λ is the attenuation length

Attenuation length for CR-induced secondary protons (and neutrons):

$$\lambda_{GCR} \sim 130~{
m g~cm^{-2}}$$
 $\lambda_{SCR} \sim 100~{
m g~cm^{-2}}$

⇒ attenuation length defines barometric coefficient of neutron monitors!

Dependence on primary zenith angle



Dependence of the contribution to the total neutron monitor count rate on the zenith angle of the primary cosmic radiation at the top of the atmosphere

Ion Production in the Earth's Atmosphere

Electromagnetic radiation from the Sun and inciendent galactic and solar cosmic rays (GCR and SCR) are ionising the Earth's atmosphere.

The energy flux of GCR falling on the Earth's atmosphere is about 10⁸ times smaller in comparison with solar electromagnetic irradiation

But: at altitudes $h \sim 3$ to 35 km, cosmic rays are the main ionising contributor



Ion production and ion concentration in the Earth's atmosphere

Ion production rate, q:

$$q = I \cdot \frac{\rho \cdot \sigma}{M}$$

where	
$I = I(h, R_c, > Phi)$	cosmic ray flux at altitude h
ho	air density
σ	effective ionisation cross section
	$pprox 2 \cdot 10^{-18} \ \mathrm{cm^2}$ at $h \leq 20 \ \mathrm{km}$
M	average mass of air atom

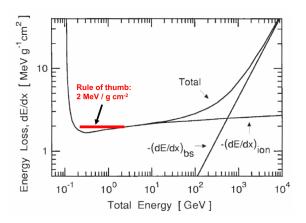
Ion concentration, n:

$$q = \alpha \cdot n^2$$

where α is the recombination coefficient

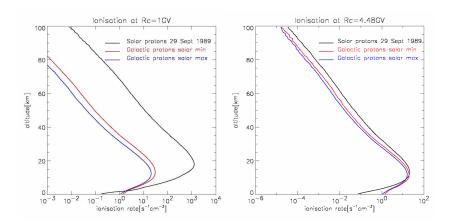


Ionisation



Energy loss of muons by electromagnetic interactions versus its total energy.

Ionisation in the atmosphere by SCR



Desorgher et al., AOGS 2004



- 1 GeV =
- 1 GV proton = MeV
- typical $B_{IMF} = nT$
- $B_{Earth} =$ Gauss
- K_p-index?

- Cutoff rigidity at geomagnetic aeuquator?
- Cutoff rigidity at high latitudes?

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- typical $B_{IMF} = 5 \text{ nT}$
- $B_{Earth} = 0.3-0.6$ Gauss
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- Most abundant component of secondary cosmic rays?
- Most abundant component at ground?
- Mean life times of pions and muons?
- Pfotzer maximum? At which altitude?

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